# EE 508

Lecture 33

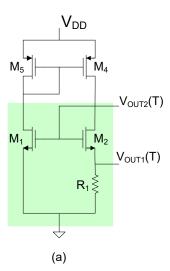
Oscillators, VCOs, and Oscillator/VCO-Derived Filters

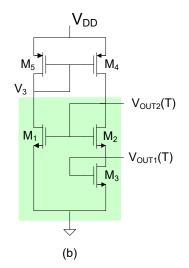
#### Review from last lecture:

#### Only two of these circuits are useful directly as bias generators!

Inverse Widlar

Not stable equilibrium point!





#### Inverse Widlar

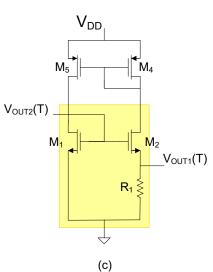
$$V_{01} = V_{Tn} \left( \frac{1 - \sqrt{\frac{W_2 L_1}{M_{IW} W_1 L_2}}}{1 + \sqrt{\frac{W_2 L_3}{W_3 L_2}} - \sqrt{\frac{W_2 L_1}{M_{IW} W_1 L_2}}} \right)$$

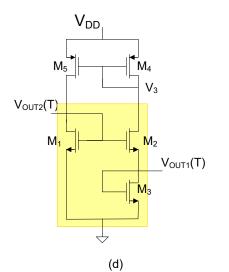
$$V_{02} = V_{Tn} \left( \frac{1 + \sqrt{\frac{W_2 L_3}{W_3 L_2}} - 2\sqrt{\frac{W_2 L_1}{M_{IW} W_1 L_2}}}{1 + \sqrt{\frac{W_2 L_3}{W_3 L_2}} - \sqrt{\frac{W_2 L_1}{M_{IW} W_1 L_2}}} \right)$$



$$\begin{split} V_{01} = & \left(\frac{\theta_l}{2} \pm \sqrt{\frac{\theta_l V_{Tn}}{2} + \left(\frac{\theta_l}{2}\right)^2}\right) \left(1 - \sqrt{\frac{W_l L_2}{M_W W_2 L_1}}\right) \\ V_{02} = & V_{Tn} + \frac{\theta_l}{2} \pm \sqrt{\frac{\theta_l V_{Tn}}{2} + \left(\frac{\theta_l}{2}\right)^2} \end{split}$$

$$I_{D1} = M_W I_{D2}$$
$$\theta_1 = \frac{M_W 2L_1}{R\mu_n C_{OX} W_1}$$



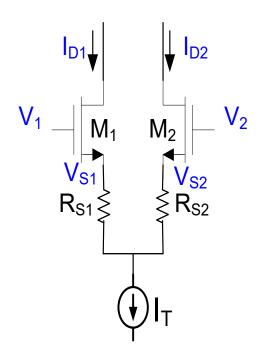


Widlar

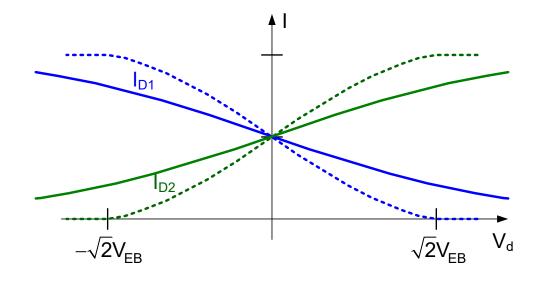
Not stable equilibrium point!

#### Review from last lecture:

#### Transconductance Linearization Strategies



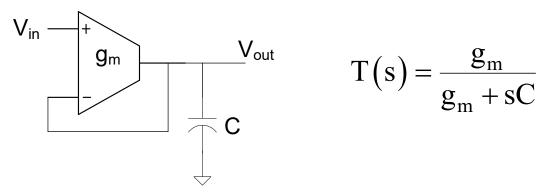
$$\sqrt{\frac{1}{\beta}} \left( \sqrt{I_T - I_{D1}} - \sqrt{I_{D1}} \right) + R_S \left( I_T - 2I_{D1} \right) = V_d$$



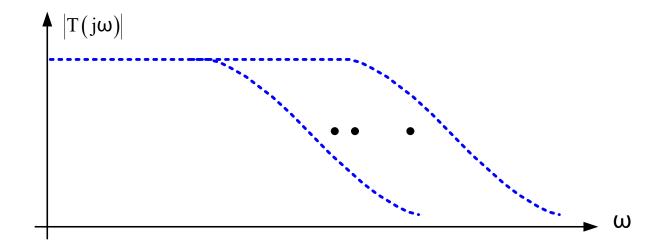
#### Review from last lecture:

# Programmable Filter Structures

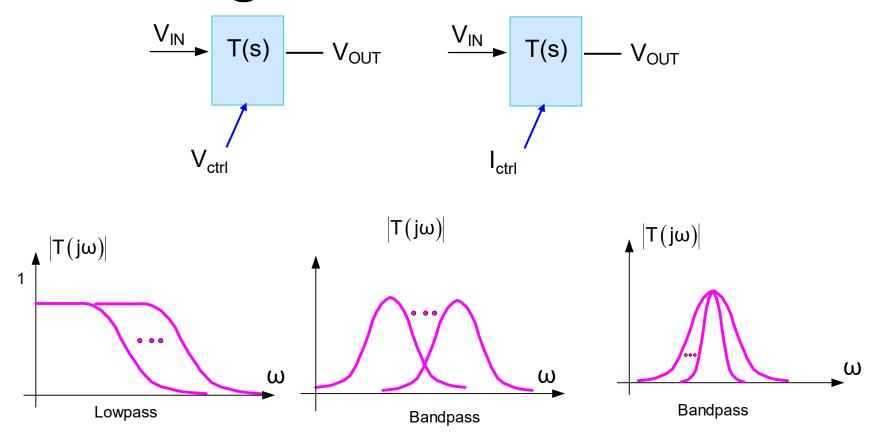
It will be assumed that the transconductance gain can be programmed with either a dc current or a dc voltage



Programmable First-Order Low-Pass Filter



# Voltage-controlled Filters

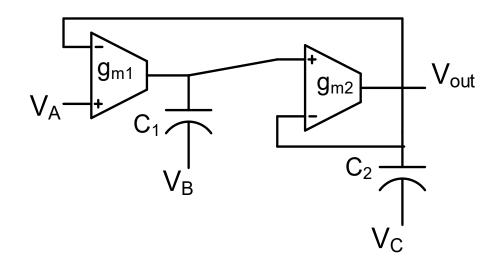


Filter characteristics can be controlled by an analog voltage  $(V_{CTRL})$  an analog current  $(I_{CTRL})$ , or a Boolean signal

Much more controllability than with a potentiometer

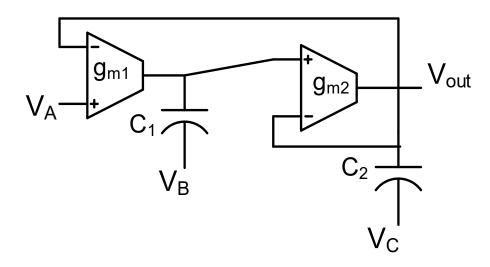
Useful when microntroller manages a signal path requiring filters

It will be assumed that the transconductance gain can be programmed with either a dc current or a dc voltage



$$V_{OUT} = \frac{s^2 C_1 C_2 V_C + s C_1 g_{m2} V_B + g_{m1} g_{m2} V_A}{s^2 C_1 C_2 + s C_1 g_{m2} + g_{m1} g_{m2}}$$

It will be assumed that the transconductance gain can be programmed with either a dc current or a dc voltage

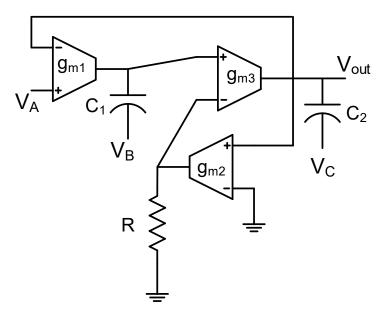


$$V_{OUT} = \frac{s^2 C_1 C_2 V_C + s C_1 g_{m2} V_B + g_{m1} g_{m2} V_A}{s^2 C_1 C_2 + s C_1 g_{m2} + g_{m1} g_{m2}}$$

$$\omega_0 = \sqrt{\frac{g_{m1}g_{m2}}{C_1C_2}}$$

$$O = \sqrt{\frac{C_2}{C_2} \sqrt{\frac{g_{m1}}{C_1C_2}}}$$

It will be assumed that the transconductance gain can be programmed with either a dc current or a dc voltage

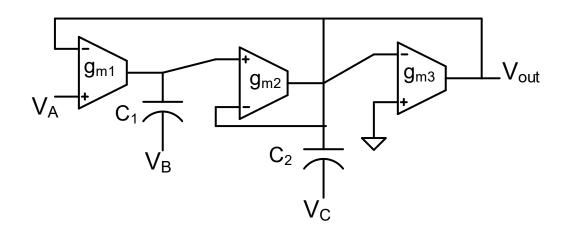


$$V_{OUT} = \frac{s^2C_1C_2V_C + sC_1g_{m2}V_B + g_{m1}g_{m2}V_A}{s^2C_1C_2 + sC_1g_{m2}g_{m3}R + g_{m1}g_{m2}}$$

$$\omega_{0} = \sqrt{\frac{g_{m1}g_{m2}}{C_{1}C_{2}}}$$

$$Q = \frac{1}{g_{m3}R} \sqrt{\frac{C_{2}g_{m1}}{C_{1}g_{m2}}}$$

It will be assumed that the transconductance gain can be programmed with either a dc current or a dc voltage

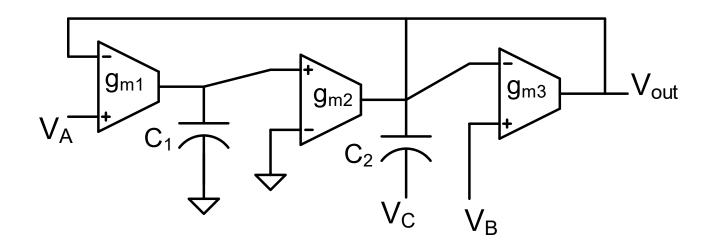


$$V_{OUT} = \frac{s^2 C_1 C_2 V_C + s C_1 g_{m2} V_B + g_{m1} g_{m2} V_A}{s^2 C_1 C_2 + s C_1 g_{m3} + g_{m1} g_{m2}}$$

$$\omega_{0} = \sqrt{\frac{g_{m1}g_{m2}}{C_{1}C_{2}}}$$

$$Q = \sqrt{\frac{C_{2}}{C_{1}}} \frac{\sqrt{g_{m1}g_{m2}}}{g_{m3}}$$

It will be assumed that the transconductance gain can be programmed with either a dc current or a dc voltage

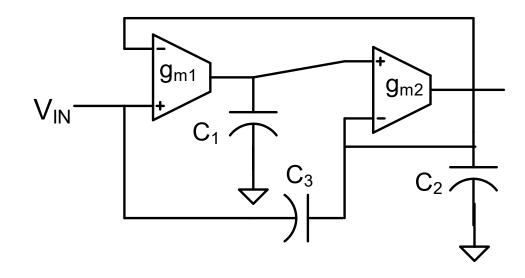


$$V_{OUT} = \frac{s^2 C_1 C_2 V_C + s C_1 g_{m3} V_B + g_{m1} g_{m2} V_A}{s^2 C_1 C_2 + s C_1 g_{m3} + g_{m1} g_{m2}}$$

$$\omega_{0} = \sqrt{\frac{g_{m1}g_{m2}}{C_{1}C_{2}}}$$

$$Q = \sqrt{\frac{C_{2}}{C_{1}}} \frac{\sqrt{g_{m1}g_{m2}}}{g_{m3}}$$

It will be assumed that the transconductance gain can be programmed with either a dc current or a dc voltage



$$T(s) = \frac{C_2}{C_2 + C_3} \frac{s^2 C_1 C_2 + g_{m1} g_{m2}}{s^2 C_1 C_2 + s g_{m2} \frac{C_1 C_2}{C_2 + C_3} + g_{m1} g_{m2} \frac{C_2}{C_2 + C_3}}$$

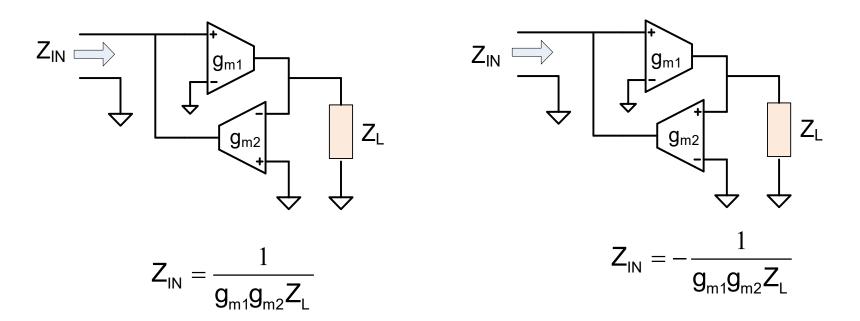
$$\omega_0 = \sqrt{\frac{g_{m1}g_{m2}}{C_1(C_2 + C_3)}}$$

$$Q = \sqrt{\frac{(C_2 + C_3)}{C_3}} \sqrt{\frac{g_{m1}}{G_3}}$$

Programmable Notch Filter (Can be used as a programmable elliptic filter)

# Programmable Filter Components

It will be assumed that the transconductance gain can be programmed with either a dc current or a dc voltage

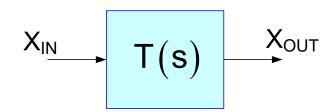


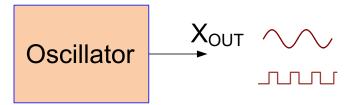
If  $Z_L$  is a capacitor serve as either positive or negative programmable inductors

Many other useful programmable filter components and filter structures possible

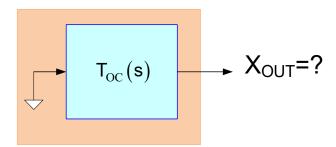
### Question:

What is the relationship, if any, between a filter and an oscillator or VCO?

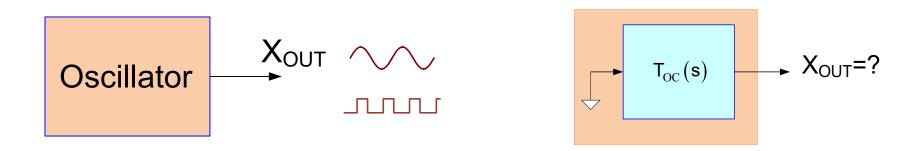




i.e. Can an oscillator be viewed as a filter with no input?



# What is the relationship, if any, between a filter and an oscillator or VCO?



Will focus on modifying oscillator structures to form high frequency narrowband filters

Claim: Narrow band filters are dependent primarily on the poles close to the imaginary axis and affected little by poles that are farther away

Goal: Obtain very high frequency filter structures

What is the relationship, if any, between a filter and an oscillator or VCO?

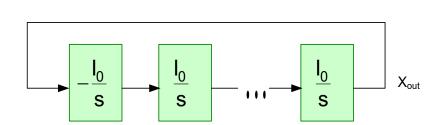


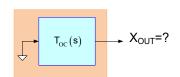
- When power is applied to an oscillator, it initially behaves as a small-signal linear network
- When operating linearly, the oscillator has poles (but no zeros)
- Poles are ideally on the imaginary axis or appear as cc pairs in the RHP
- There is a wealth of literature on the design of oscillators
- Oscillators often are designed to operate at very high frequencies
- If cc poles of a filter are moved to RHP it will become an oscillator
- If RHP poles of an oscillator are moved to the LHP it will become a filter if an input is applied
- Can oscillators be modified to become filters?

# Oscillator Background:

Consider a cascaded integrator loop comprised of n integrators

This structure is often used to build oscillators





(assume an odd number of inverting integrators)

$$X_{OUT} = -\left(\frac{I_0}{s}\right)^n X_{OUT}$$
$$X_{OUT} \left(s^n + I_0^n\right) = 0$$
$$D(s) = s^n + I_0^n$$

### Consider the poles of

$$D(s) = s^n + I_0^n$$

$$s^n + I_0^n = 0$$

$$s^n = -I_0^n$$

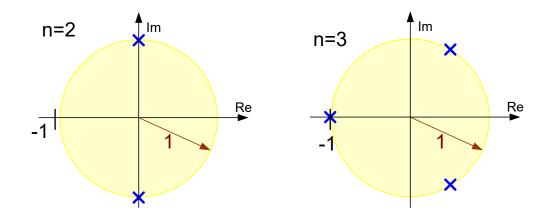
$$\mathbf{s} = \left[ -I_0^{\mathsf{n}} \right]^{\frac{1}{n}}$$

$$\mathbf{s} = \begin{bmatrix} -1 \end{bmatrix}^{\frac{1}{n}} \begin{bmatrix} I_0^n \end{bmatrix}^{\frac{1}{n}}$$

$$\mathbf{s} = I_0 \left[ -1 \right]^{\frac{1}{n}}$$

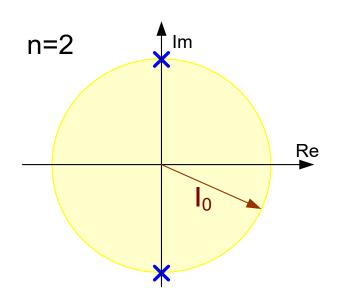
Poles are the n roots of -1 scaled by I<sub>0</sub>

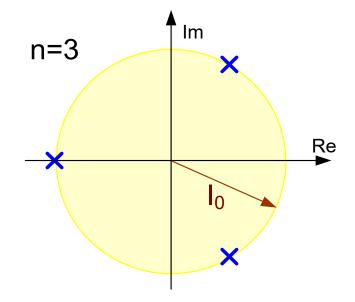
Roots of -1:

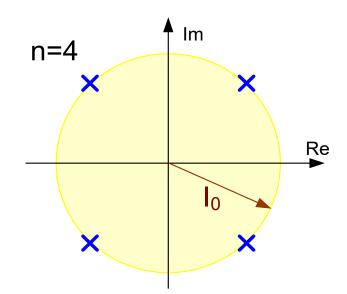


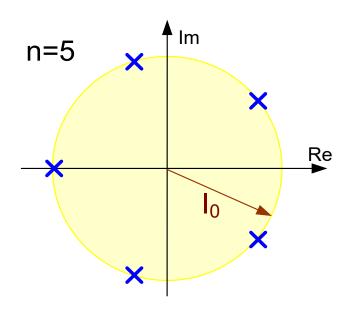
Roots are uniformly spaced on a unit circle

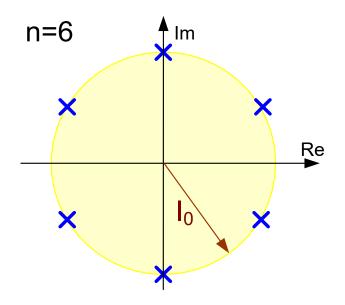
# Consider the poles of $D(s) = s^n + I_0^n$

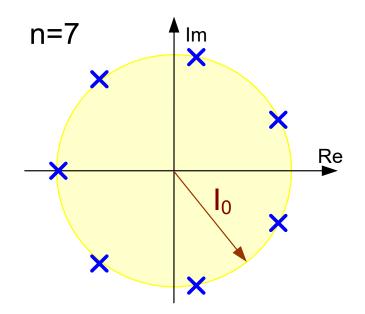


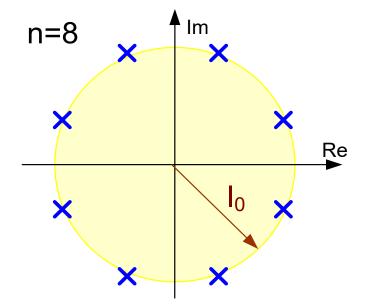












### Some useful theorems

Theorem: A rational fraction 
$$T(s) = \frac{N(s)}{\prod_{i=1}^{n} (s-p_i)}$$
 with simple poles can be expressed

in partial fraction form as 
$$T(s) = \sum_{i=1}^{n} \frac{A_i}{s - p_i}$$

where 
$$A_i = (s-p_i)T(s)|_{s=p_i}$$
 for  $1 \le j \le n$ 

Theorem: The impulse response of a rational fraction T(s) with simple poles can be expressed as  $r(t) = \sum_{i=1}^{n} A_i e^{p_i t}$  where the numbers  $A_i$  are the coefficients

in the partial fraction expansion of T(s)

Theorem: If  $p_i$  is a simple complex pole of the rational fraction T(s), then the partial fraction expansion terms in the impulse response corresponding to  $p_i$  and  $p_i^*$  can be expressed as  $\frac{A_i}{s - p_i} + \frac{A_i^*}{s - p_i^*}$ 

Theorem: If  $p_i = \alpha_i + j\beta_i$  is a simple pole with non-zero imaginary part of the rational fraction T(s), then the impulse response terms corresponding to the poles  $p_i$  and  $p_i$  in the partial fraction expansion can be expressed as

$$|A_i|e^{\alpha_i t}\cos(\beta_i t + \theta_i)$$

where  $\theta_i$  is the angle of the complex quantity  $A_i$ 

Observe r(t) term corresponding to any complex pole pair is real!

Theorem: If all poles of an n-th order rational fraction T(s) are simple and have a non-zero Imaginary part, then the impulse response can be expressed as

$$\sum_{i=1}^{n/2} |A_i| e^{\alpha_i t} \cos(\beta_i t + \theta_i)$$

where  $\theta_i$ ,  $A_{i,\alpha_i}$ , and  $\beta_i$  are as defined before

Theorem: If an odd-order rational fraction has one pole on the negative real axis at  $\alpha_0$  and n simple poles that have a non-zero Imaginary part, then the impulse response can be expressed as

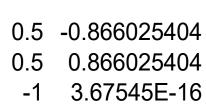
$$A_0 e^{\alpha_0 t} + \sum_{i=1}^{n/2} |A_i| e^{\alpha_i t} \cos(\beta_i t + \theta_i)$$

where  $\theta_i$ ,  $A_i \alpha_i$ , and  $\beta_i$  are as defined before

Observe r(t) is real for both even and odd n!

# Consider the following 3-pole situation

Poles of 
$$D(s) = s^n + I_0^n$$



n=3  $\begin{array}{c}
h = 60^{\circ} \\
\alpha = I_{0}\cos(60^{\circ}) \\
\beta = I_{0}\sin(60^{\circ})
\end{array}$ 

10

for cc pole pair:

$$\alpha = 0.5 I_0$$

$$\beta = 0.866 I_0$$

Oscillatory output at startup with any small impulse input:

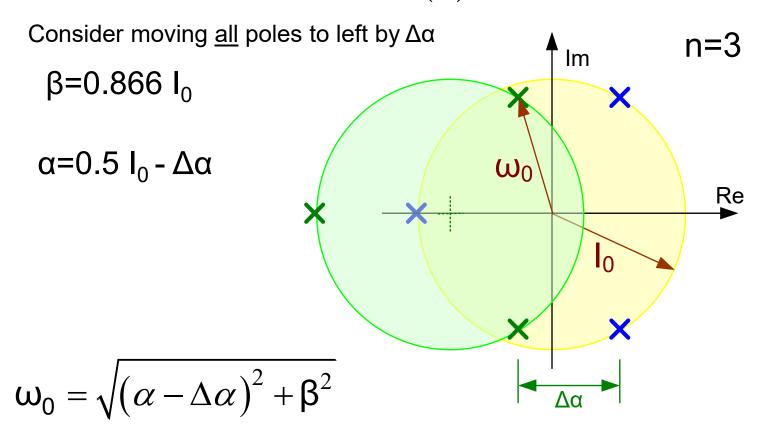
$$|A_i|e^{\alpha_i t}\cos(\beta_i t + \theta_i)$$

Re

Starts at ω=0.866I<sub>0</sub> and will slow down as nonlinearities limit amplitude

# Consider the following 3-pole situation

Poles of 
$$D(s) = s^n + I_0^n$$



So, to get a high  $\omega_0$ , want  $\beta$  as large as possible

#### Consider now the filter obtained by adding a loss of $\alpha_L$ to the integrators

Will now determine  $\alpha_L$  and  $I_0$  needed to get a desired pole Q and  $\omega_0$  by moving all poles so that right-most pole pair is dominant high-frequency pole pair of filter

The values of  $\alpha$  and  $\beta$  are dependent upon  $I_0$  but the angle  $\theta$  is only dependent upon the number of integrators in the oscillator or VCO

$$\alpha + j\beta = I_0(\cos\theta + j\sin\theta)$$

Define the location of the filter pole to be

$$\alpha_F + j\beta_F$$

It follows that

$$\beta_F = \beta$$
  $\alpha_F = \alpha - \alpha_L$ 

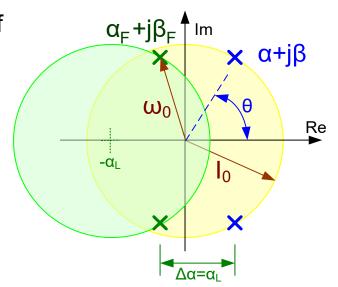
The relationship between the filter parameters is well known

$$\beta_{F} = \frac{\omega_{0}}{2Q} \sqrt{4Q^{2}-1} \qquad \alpha_{F} = -\frac{\omega_{0}}{2Q}$$

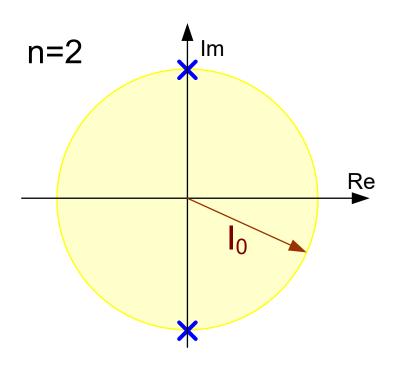
Thus for any n

$$I_0 = \frac{\omega_0}{(\sin\theta)2Q} \sqrt{4Q^2 - 1}$$

$$I_0 = \frac{\omega_0}{(\sin\theta)2Q} \sqrt{4Q^2 - 1}$$
  $\alpha_L = \frac{\omega_0}{2Q} + I_0 \cos\theta = \frac{\omega_0}{2Q} + \frac{\omega_0}{2Q(\tan\theta)} \sqrt{4Q^2 - 1}$ 



#### Will a two-stage structure give the highest frequency of operation?

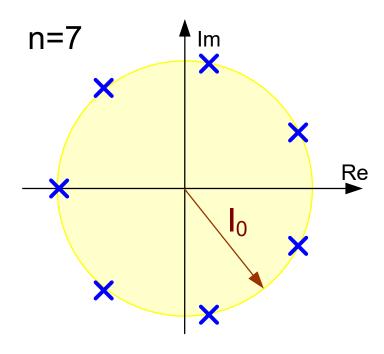


$$\omega_0 = \sqrt{(\alpha - \Delta \alpha)^2 + \beta^2}$$
  $\omega_0 = \sqrt{(-\Delta \alpha)^2 + \beta^2}$ 

- Even though the two-stage structure may not oscillate, can work as a filter!
- Need odd number of inversions in integrators
- Can add phase lead if necessary

# Oscillator Background:

What will happen with a circuit that has two pole-pairs in the RHP?

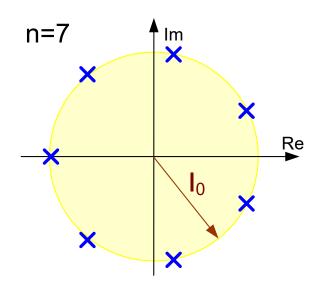


General form of response for odd number of poles:

$$A_0 e^{\alpha_{_{\scriptscriptstyle 0}} t} + \textstyle\sum\limits_{i=1}^{n/2} \left|A_i\right| e^{\alpha_{_i} t} cos \left(\beta_i t + \theta_i\right)$$

The impulse response (for n=7) will have two decaying exponential terms and two growing exponential terms

#### What will happen with a circuit that has two pole-pairs in the RHP?



$$\alpha_1$$
=0.2225  $\beta_1$ =0.974

$$\alpha_2$$
=0.9009  $\beta_2$ =0.4338

Consider the growing exponential terms and normalize to  $I_0=1$ 

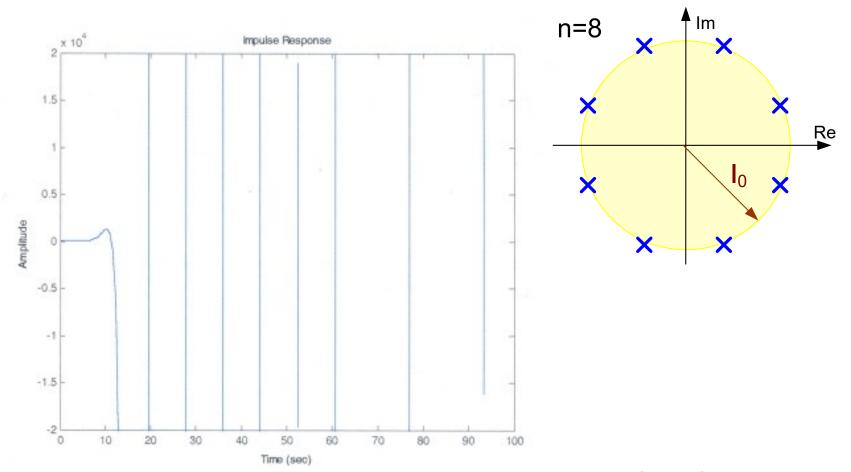
$$|A_1|e^{\alpha_1 t}\cos(\beta_1 t+\theta_1) + |A_2|e^{\alpha_2 t}\cos(\beta_2 t+\theta_2)$$

At t=145 (after only 10 periods of the lower frequency signal)

$$r = \frac{e^{\alpha_2 t}}{e^{\alpha_1 t}}\bigg|_{t=1.45} = \frac{e^{.9009 \cdot 145}}{e^{.2225 \cdot 145}} = 5.2x10^{42}$$

The lower frequency oscillation will completely dominate!

#### What will happen with a circuit that has two pole-pairs in the RHP?



Thanks to Chen for these plots

Figure 14 N=8 impulse response

Can only see the lower frequency component!

#### What will happen with a circuit that has two pole-pairs in the RHP?

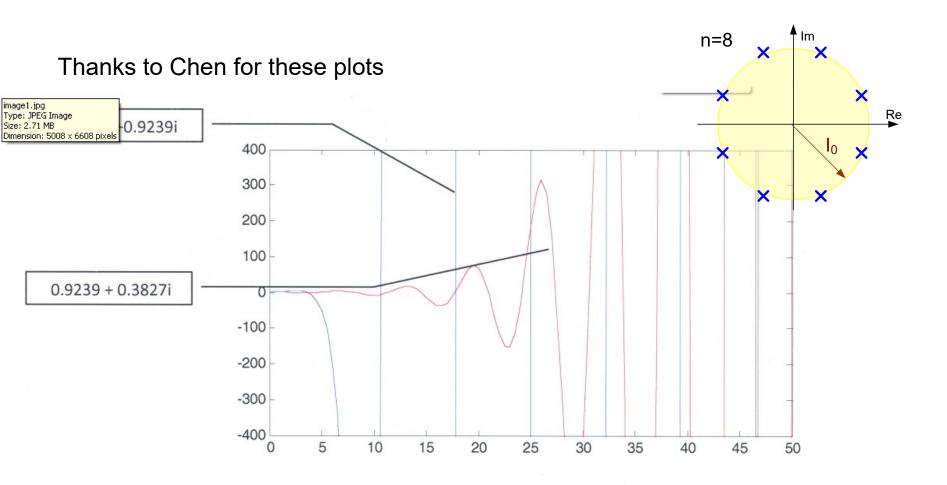
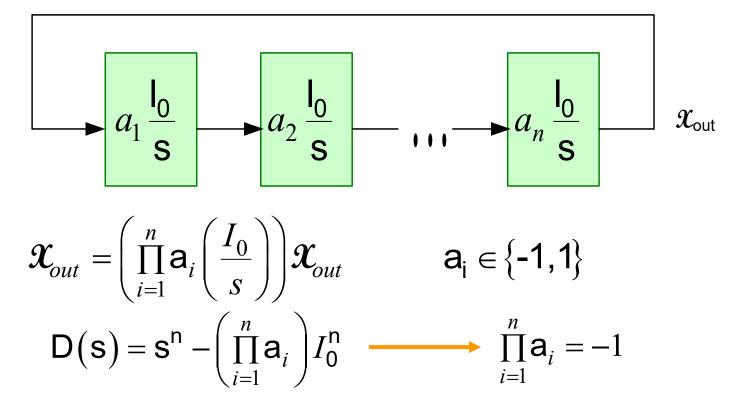


Figure 7 N=8 the impulse response of two poles

After even only two periods of the lower frequency waveform, it completely dominates!

#### How do we guarantee that we have a net coefficient of +1 in D(s)?

$$D(s) = s^n + I_0^n$$

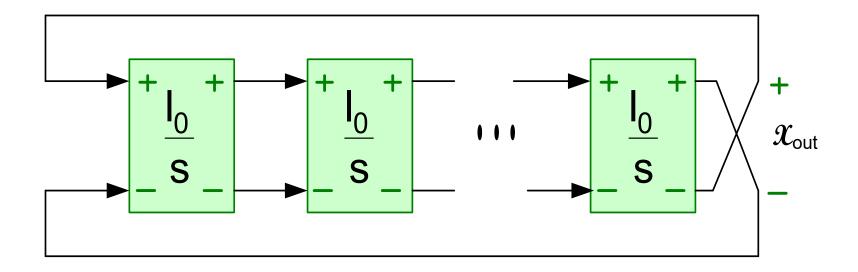


Must have an odd number of inversions in the loop!

If n is odd, all stages can be inverting and identical!

#### How do we guarantee that we have a net coefficient of +1 in D(s)?

$$D(s) = s^n + I_0^n$$



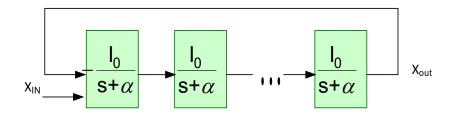
If fully differential or fully balanced, must have an odd number of crossings of outputs

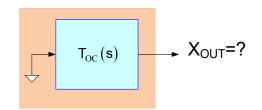
Applicable for both even and odd order loops

# Inputs to Oscillator-Derived Filters:

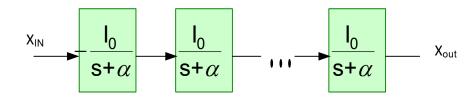
Most applicable to designing 2<sup>nd</sup>-order high frequency narrow band filters

- Add loss to delay stages
- Multiple Input Locations Often Possible
- Natural Input is Input to delay stage

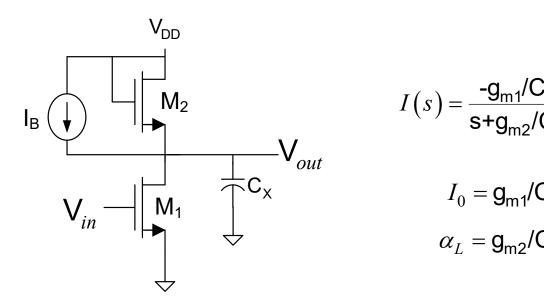




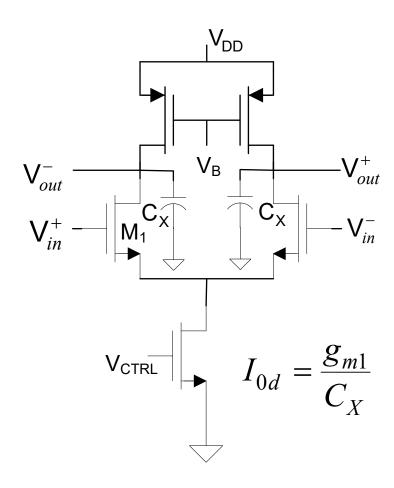
- Add loss to delay stages
- Often Just Salvage Stages (drop feedback loop)
- Natural input is input to delay stage



#### A lossy integrator stage

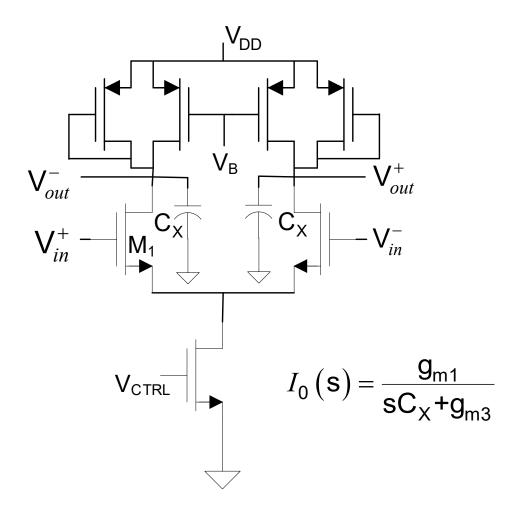


#### A fully-differential voltage-controlled integrator stage



Will need CMFB circuit

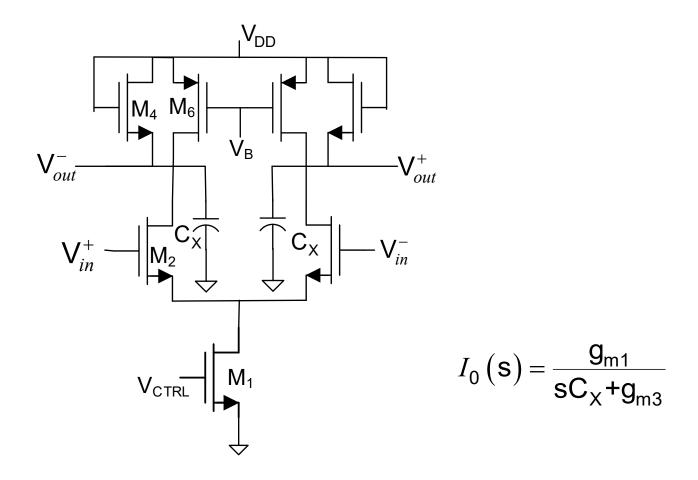
#### A fully-differential voltage-controlled integrator stage with loss



Will need CMFB circuit

#### A fully-differential voltage-controlled integrator stage with loss

(almost same as previous)



Will need CMFB circuit

Using the single-stage lossy integrator, design the integrator to meet a given  $\omega_0$  and Q requirement

Recall:

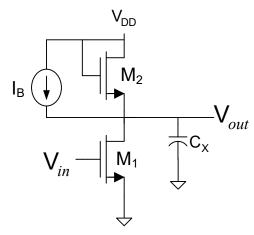
$$I_0 = \frac{\omega_0}{(\sin\theta) 2Q} \sqrt{4Q^2 - 1}$$

$$\alpha_L = \frac{\omega_0}{2Q} + \frac{\omega_0}{2Q(\tan\theta)} \sqrt{4Q^2 - 1}$$
(2)

Substituting for  $I_0$  and  $\alpha_L$  we obtain:

$$\frac{g_{m1}}{C_{X}} = \frac{\omega_{0}}{(\sin\theta)2Q} \sqrt{4Q^{2}-1}$$

$$\frac{g_{m2}}{C_{X}} = \frac{\omega_{0}}{2Q} + \frac{\omega_{0}}{2Q(\tan\theta)} \sqrt{4Q^{2}-1}$$
(3)
$$(3)$$



$$I_0 = g_{m1}/C_X$$

$$\alpha_L = g_{m2}/C_X$$

Using the single-stage lossy integrator, design the integrator to meet a given

 $\omega_0$  and Q requirement

Expressing  $g_{m1}$  and  $g_{m2}$  in terms of design parameters:

$$\frac{\mu C_{OX} W_1 V_{EB1}}{L_1 C_X} = \frac{\omega_0}{(\sin \theta) 2Q} \sqrt{4Q^2 - 1}$$

$$\frac{\mu C_{\text{OX}} W_2 V_{\text{EB2}}}{L_2 C_X} = \frac{\omega_0}{2Q} + \frac{\omega_0}{2Q \left( tan\theta \right)} \sqrt{4Q^2 - 1}$$

If we assume  $I_B=0$ , equating drain currents obtain:

$$V_{EB2} = V_{EB1} \sqrt{\frac{W_1 L_2}{W_2 L_1}}$$
 (7)

Thus the previous two expressions can be rewritten as:

$$\frac{\mu C_{OX} V_{EB1}}{C_{X}} \left[ \frac{W_{1}}{L_{1}} \right] = \frac{\omega_{0}}{(\sin \theta) 2Q} \sqrt{4Q^{2}-1} \qquad (8)$$

$$\frac{\mu C_{OX} V_{EB1}}{C_{X}} \left[ \frac{W_{1} W_{2}}{L_{1} L_{2}} \right] = \frac{\omega_{0}}{2Q} + \frac{\omega_{0}}{2Q(\tan \theta)} \sqrt{4Q^{2}-1} \qquad (9)$$

$$V_{in} = \begin{bmatrix} M_2 \\ M_1 \end{bmatrix}$$

$$V_{out}$$

$$I_0 = g_{m1}/C_X$$

$$\alpha_L = g_{m2}/C_X$$

Using the single-stage lossy integrator, design the integrator to meet a given

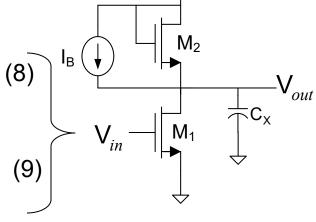
 $\omega_0$  and Q requirement

$$\frac{\mu C_{OX} V_{EB1}}{C_{X}} \left[ \frac{W_{_{1}}}{L_{_{1}}} \right] = \frac{\omega_{0}}{\left( sin\theta \right) 2Q} \sqrt{4Q^{2}-1}$$

$$\frac{\mu C_{OX} V_{EB1}}{C_X} \left[ \frac{W_1 W_2}{L_1 L_2} \right] = \frac{\omega_0}{2Q} + \frac{\omega_0}{2Q (\tan \theta)} \sqrt{4Q^2 - 1}$$

Taking the ratio of these two equations we obtain:

$$\frac{W_2}{L_2} = \frac{\sin\theta + \cos\theta\sqrt{4Q^2 - 1}}{\sqrt{4Q^2 - 1}}$$
 (10)



$$I_0 = g_{m1}/C_X$$

$$\alpha_L = g_{m2}/C_X$$

Observe that the pole Q is determined by the dimensions of the lossy device!

Using the single-stage lossy integrator, design the integrator to meet a given

 $\omega_0$  and Q requirement

$$\frac{\mu C_{OX} V_{EB1}}{C_{X}} \left[ \frac{W_{1}}{L_{1}} \right] = \frac{\omega_{0}}{\left( \sin \theta \right) 2Q} \sqrt{4Q^{2}-1}$$

$$\frac{W_{2}}{L_{2}} = \frac{\sin \theta + \cos \theta \sqrt{4Q^{2}-1}}{\sqrt{4Q^{2}-1}}$$
(10)

Still must obtain  $W_1/L_1$ ,  $V_{EB1}$ , and  $C_X$  from either of these equations

Although it appears that there might be 3 degrees of freedom left and only one constraint (one of these equations), if these integrators are connected in a loop, the operating point (Q-point) will be the same for all stages and will be that value where  $V_{out}=V_{in}$ . So, this adds a second constraint.

Setting  $V_{out}=V_{in}$ , and assuming  $V_{T1}=V_{T2}$ , we obtain from KVL

$$V_{DD} = V_{EB1} + V_{EB2} + 2V_{T}$$
 (11)

But  $V_{EB1}$  and  $V_{EB2}$  are also related in (7)

Using the single-stage lossy integrator, design the integrator to meet a given  $\omega_0$  and Q requirement

$$\frac{\mu C_{OX} V_{EB1}}{C_{X}} \left[ \frac{W_{1}}{L_{1}} \right] = \frac{\omega_{0}}{\left( \sin \theta \right) 2Q} \sqrt{4Q^{2}-1}$$

$$\frac{W_{2}}{L_{2}} = \frac{\sin \theta + \cos \theta \sqrt{4Q^{2}-1}}{\sqrt{4Q^{2}-1}}$$
(10)

Still must obtain  $W_1/L_1$ ,  $V_{EB1}$ , and  $C_X$  from either of these equations

$$V_{DD} = V_{EB1} + V_{EB2} + 2V_{T}$$

$$V_{EB1} = \frac{V_{DD} - 2V_{T}}{1 + \sqrt{\frac{W_{1}L_{2}}{W_{1}L_{2}}}}$$

$$(12)$$

Substituting (10) into (12) and then into (8) we obtain

$$\frac{\mu C_{OX}}{C_{X}} \left[ \frac{W_{1}}{L_{1}} \right] \left( \frac{V_{DD} - 2V_{T}}{1 + \sqrt{\left(\frac{W_{1}}{L_{1}}\right)^{-1} \left(\frac{\sin\theta + \cos\theta\sqrt{4Q^{2} - 1}}{\sqrt{4Q^{2} - 1}}\right)}} \right) = \frac{\omega_{0}}{(\sin\theta)2Q} \sqrt{4Q^{2} - 1} \tag{13}$$

Using the single-stage lossy integrator, design the integrator to meet a given  $\omega_0$  and Q requirement

$$\frac{W_{2}}{L_{2}} = \frac{\sin\theta + \cos\theta\sqrt{4Q^{2}-1}}{\sqrt{4Q^{2}-1}}$$

$$\frac{\mu C_{OX}}{C_{X}} \left[\frac{W_{1}}{L_{1}}\right] \frac{V_{DD} - 2V_{T}}{1 + \sqrt{\left(\frac{W_{1}}{L_{1}}\right)^{-1} \left(\frac{\sin\theta + \cos\theta\sqrt{4Q^{2}-1}}{\sqrt{4Q^{2}-1}}\right)}} = \frac{\omega_{0}}{(\sin\theta)2Q} \sqrt{4Q^{2}-1}$$
(10)

There is still one degree of freedom remaining. Can either pick  $W_1/L_1$  and solve for  $C_X$  or pick  $C_X$  and solve for  $W_1/L_1$ .

Explicit expression for W<sub>1</sub>/L<sub>1</sub> not available

Tradeoffs between C<sub>x</sub> and W<sub>1</sub>/L<sub>1</sub> will often be made

Since  $V_{OUTQ}=V_T+V_{EB1}$ , it may be preferred to pick  $V_{EB1}$ , then solve (12) for  $W_1/L_1$  and then solve (13) for  $C_X$ 

Adding  $I_B$  will provide one additional degree of freedom and will relax the relationship between  $V_{OUTQ}$  and  $W_1/L_1$  since (7) will be modified



Stay Safe and Stay Healthy!

# End of Lecture 33